

Models for Quantifying Risk --Sixth Edition
Solutions Manual
 Errata List
 September 19, 2014

Page 121:

Beginning with the ninth line, the one immediately following the long centered equation, the solution should read:

“As expected, the left side integrates to ${}_n p_{xy}^{03}$, since ${}_0 p_{xy}^{03} = 0$. The challenge is now to translate the terms on the right side, which are written in multi-state model notation, into the actuarial notation defined for the common shock model in Section 12.7. Clearly ${}_t p_{xy}^{00}$ translates to ${}_t p_{xy}$, the probability that both (x) and (y) have survived against all hazard forces, and $\mu_{x+t;y+t}^{03}$ translates to λ , the common shock force of failure to which both (x) and (y) are subject. The term ${}_t p_{xy}^{01}$ is the probability that (x) is alive, but (y) is not, at time t . To satisfy this event, (x) must have survived all hazard factors, including the common shock ones, and (y) must have failed *due to hazard factors unique to (y)*. (If (y) had failed due to a common shock hazard factor, then (x) could not be alive.) The term μ_{x+t}^{13} is the force of failure operating on (x) after the failure of (y), so it includes only the hazard factors unique to (x), which is denoted μ_{x+t}^* in actuarial notation. The third pair of terms is similarly analyzed, with the roles of (x) and (y) reversed. Then the equation, written in common shock actuarial notation, is

$$\begin{aligned} {}_n p_{xy}^{03} &= \int_0^n \left[{}_t p_{xy} \cdot \lambda + (1 - {}_t p_y^*) \cdot {}_t p_x \mu_{x+t}^* + (1 - {}_t p_x^*) \cdot {}_t p_y \mu_{y+t}^* \right] dt \\ &= \lambda \cdot \overset{\circ}{e}_{xy:\overline{n}|} + ({}_n q_{xy}^2)^* + ({}_n q_{xy}^2)^* = {}_n q_{xy}^* + \lambda \cdot \overset{\circ}{e}_{xy:\overline{n}|}, \end{aligned}$$

as required. (Note that both $({}_n q_{xy}^2)^*$ and $({}_n q_{xy}^2)^*$ denote the failure of both persons (in opposite orders) before time n due to hazard forces unique to each person.)”